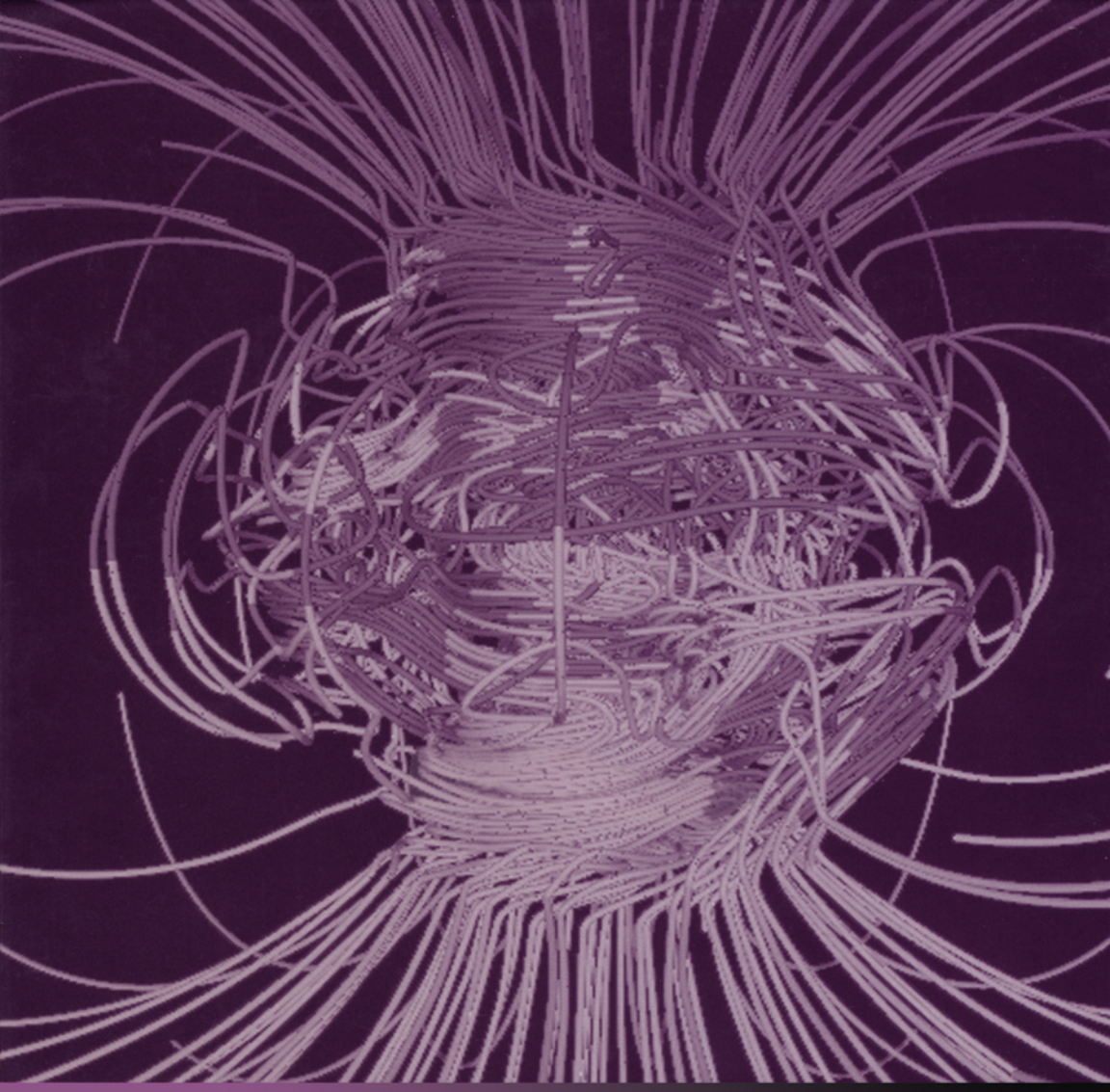

The Magnetic Field of the Earth

Paleomagnetism, the Core, and the Deep Mantle

Ronald T. Merrill *Michael W. McElhinny* *Phillip L. McFadden*

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The Magnetic Field of the Earth

Paleomagnetism, the Core, and the Deep Mantle

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The Magnetic Field of the Earth

Paleomagnetism, the Core, and the Deep Mantle

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The cover of this book shows the magnetic field for the Glatzmaier–Roberts dynamo at a time when the field is not undergoing a reversal (unpublished figure supplied to us by Glatzmaier, 1996). A change in color of the field lines indicates a change in the direction of the radial component of the magnetic field. On close inspection, the tangential cylinder is apparent in both the magnetic field (cover) and in the velocity field (Fig. 9.7).

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